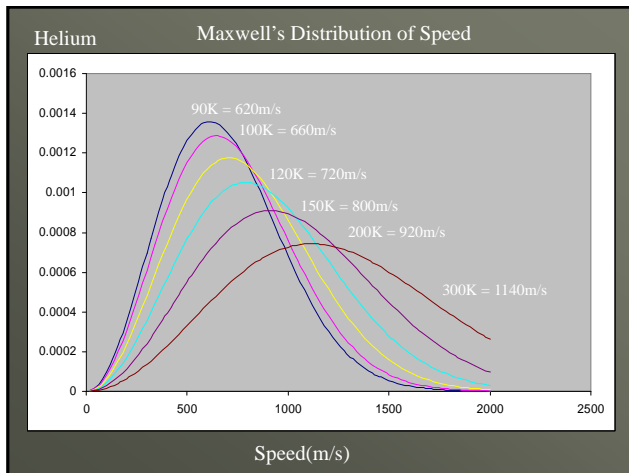
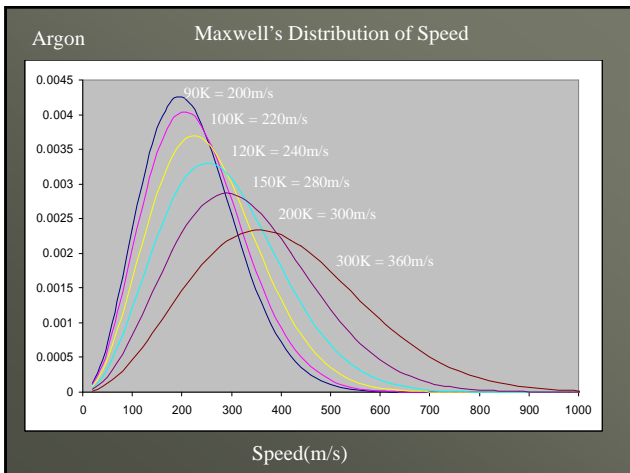
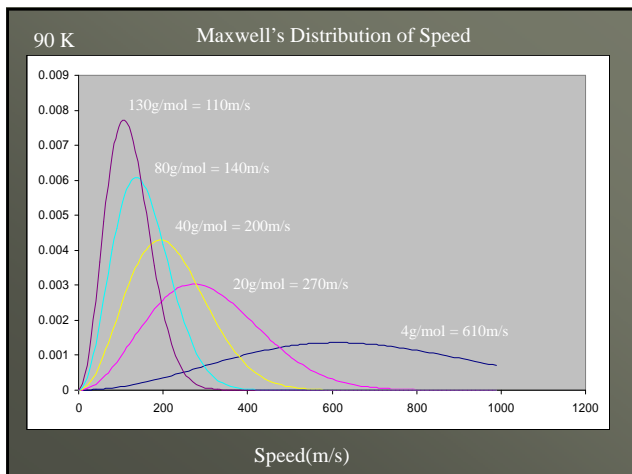


Maxwell's Distribution of Speed

$$f(s) = 4\pi \left(\frac{M}{2\pi RT} \right)^{\frac{3}{2}} s^2 e^{-\frac{Ms^2}{2RT}}$$





Collision Cross Section:

Ideal elastic hard sphere collision:

$$\Omega = \pi(r_1 + r_2)^2$$

Where Ω is the collision cross-section

$$\delta = r_1 + r_2 = \left(\frac{\Omega}{\pi}\right)^{\frac{1}{2}}$$

Where δ is the collision distance

These equations neglect potential interactions between the two molecules (attractive and repulsive), and assume spherical geometry.

Mean Free Path (λ):

#collisions per unit time:

$$Z_1 = \pi d^2 \langle v \rangle N$$

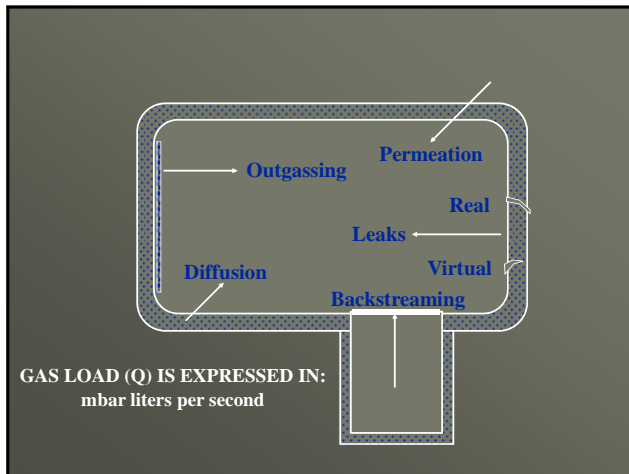
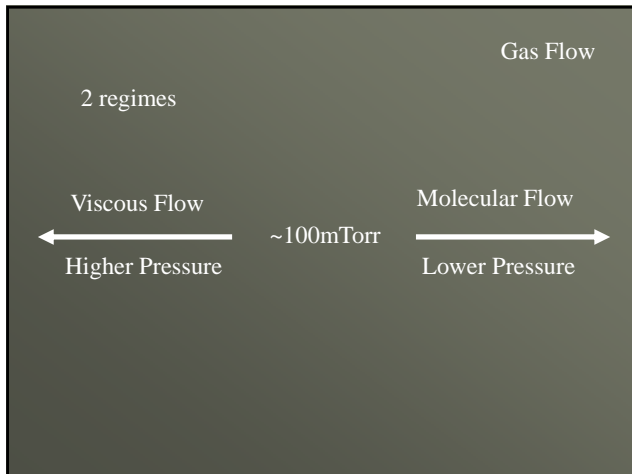
Mean free path (length b/w collisions)

$$\lambda = \frac{\langle v \rangle}{Z_1} = \frac{\langle v \rangle}{\pi(r_1 + r_2)^2 \sqrt{2} \langle v \rangle N}$$

$$\lambda = \frac{1}{\pi(r_1 + r_2)^2 \sqrt{2} N}$$

x-section	He	N2	CO2	CH4
10000	0.21	0.42	0.52	0.88 nm ²
1000	1E-08	5.07E-09	4.2E-09	2.48E-09
100	1E-07	5.07E-08	4.2E-08	2.48E-08
10	1E-06	5.07E-07	4.2E-07	2.48E-07
1	0.0001	5.07E-06	4.2E-06	2.48E-06
0.1	0.00104	0.00507	0.0042	0.00248
0.01	0.01039	0.050705	0.004197	0.00248
0.001	0.10391	0.050749	0.041965	0.024798
0.0001	1.03914	0.507496	0.419652	0.247976
0.00001	10.3914	5.074862	4.196521	2.479762
0.000001	103.914	50.74862	41.96521	24.79762
0.0000001	1039.14	507.4862	419.6521	247.9762
0.00000001	10391.4	5074.862	4196.521	2479.762
0.000000001	103914	50748.62	41965.21	24797.62
1E-10	1039139	507486.2	419652.1	247976.2
1E-11	1E+07	5074862	4196521	2479762
1E-12	1E+08	50748621	41965206	24797622
1E-13	1E+09	5.07E+08	4.2E+08	2.48E+08
1E-14	1E+10	5.07E+09	4.2E+09	2.48E+09 meters

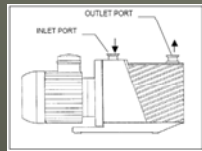
$$\lambda = \frac{5 \cdot 10^{-3} \text{ Torr} \cdot \text{cm}}{P_{\text{Torr}}}$$



Pumping Speed

$$S \equiv \frac{dV}{dt} \quad \text{L/s, m}^3/\text{s, ft}^3/\text{min (cfm)}$$

$$S_p \equiv \frac{dV}{dt}$$



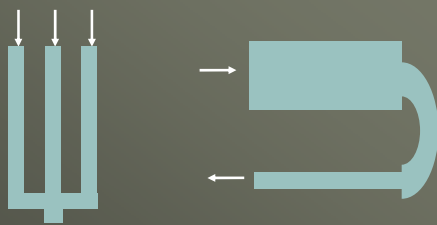
The mass rate of flow through a vacuum system is known as throughput (Q), torr L/s

$$Q \equiv PS$$

The ability of an apparatus to transmit gas is known as conductance (C), same units as pumping speed.

$$Q = (P_1 - P_2)C$$

Conductance



$$C_{parallel} = C_1 + C_2 + C_3 + \dots$$

$$C_{series} = \left[\frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots \right]^{-1}$$

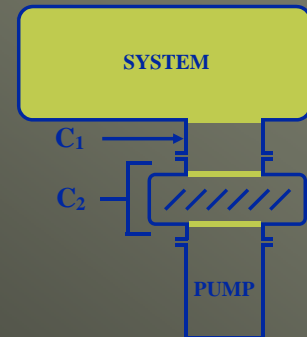
Series Conductance

$$R_T = R_1 + R_2$$

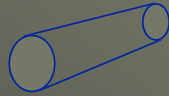
$$\frac{1}{C_T} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$\frac{1}{C_T} = \frac{C_1 + C_2}{C_1 \times C_2}$$

$$C_T = \frac{C_1 \times C_2}{C_1 + C_2}$$



Conductance in Viscous Flow



Under viscous flow conditions doubling the pipe diameter increases the conductance sixteen times.
The conductance is **INVERSELY** related to the pipe length

Viscous Flow (Long Round Tube; air)

$$C = 1.38 \times 10^2 \times \frac{d^4}{l} \times \frac{P_1 + P_2}{2} \text{ (l/sec)}$$

d = diameter of tube in cm
l = length of tube in cm
P₁ = inlet pressure in torr
P₂ = exit pressure in torr

Viscous Flow (Long Round Tube; nitrogen)

EXAMPLE:

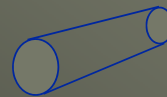
d = 4 cm P₁ = 2 torr
l = 100 cm P₂ = 1 torr

$$C = 138 \times \frac{d^4}{l} \times \frac{P_1 + P_2}{2} \text{ (liter/sec)}$$

$$C = 138 \times \frac{256}{100} \times \frac{3}{2} \text{ (liter/sec)}$$

$$C = 530 \text{ (liter/sec)}$$

Conductance in Molecular Flow



Under molecular flow conditions doubling the pipe diameter increases the conductance eight times.
The conductance is **INVERSELY** related to the pipe length.

Conductance in Molecular Flow (Long Round Tube)

$$C = 3.81 \times \frac{d^3}{l} \times \sqrt{\frac{T}{M}} \quad (\text{l/sec})$$

d = diameter of tube in cm

l = length of tube in cm

T = temperature (K)

M = A.M.U.

Conductance in Molecular Flow (Long Round Tube)

EXAMPLE:

T = 295 K (22 °C)

M = 28 (nitrogen)

$$\begin{aligned} C &= 3.81 \times \frac{d^3}{l} \times \sqrt{\frac{T}{M}} \quad (\text{l/sec}) \\ &= 3.81 \times \frac{d^3}{l} \times \sqrt{\frac{295}{28}} \\ &= 12.36 \times \frac{d^3}{l} \quad (\text{l/sec}) \end{aligned}$$

EXAMPLE:

T = 295 K (22 °C)

M = 28 (nitrogen)

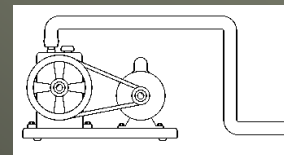
d = 4 cm

l = 100 cm

$$\begin{aligned} C &= 3.81 \times \frac{d^3}{l} \times \sqrt{\frac{T}{M}} \quad (\text{l/sec}) \\ &= 3.81 \times \frac{d^3}{l} \times \sqrt{\frac{295}{28}} \\ &= 12.36 \times \frac{d^3}{l} \quad (\text{l/sec}) \\ &= 12.36 \times 0.64 \\ &= 7.9 \quad (\text{l/sec}) \end{aligned}$$

$$Q = (P_1 - P_2)C$$

$$S_p = \frac{Q}{P_2}$$



$$S = \frac{Q}{P_1}$$

Using the conductance equation, and knowing that mass transfer is the same (Q) throughout the system; substitute the pressure values for the pumping speed at aperture and pump.

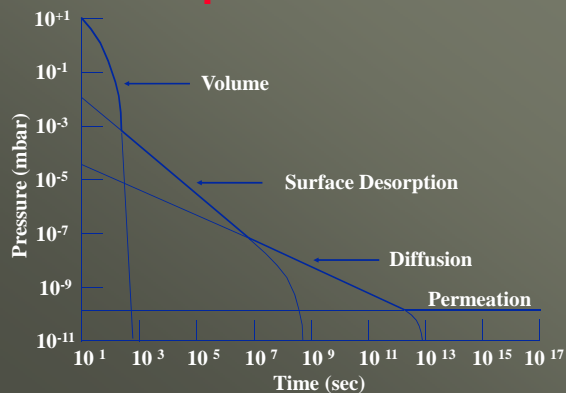
$$\frac{1}{S} = \frac{1}{S_p} + \frac{1}{C}$$

Pumpdown time

Pumpdown time is also useful info. This can identify slow leaks, outgassing, etc.

$$t = \frac{V}{S} \ln \left(\frac{P_o}{P} \right)$$

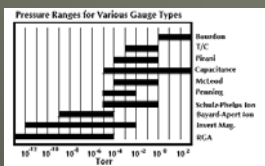
Pumpdown Curve



Pressure Gauges

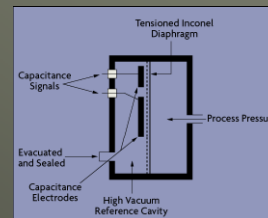
Four Major Types

1. Mechanical Gauge
2. Thermal-Conductivity
3. Viscous-Drag
4. Ionization Gauge



Capacitance Manometer

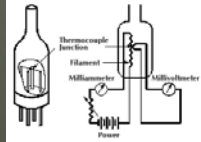
Range: 1000 Torr to 1x10⁻⁴ Torr
 Accuracy: 0.01%
 Response: 10ms



Thermal-Conductivity

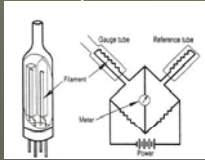
Heat loss to the surrounding gas

Direct Measurement



Thermocouple Gauge

Comparison

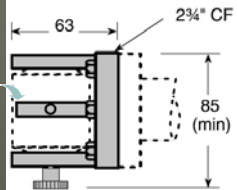


Pirani Gauge

Range: 10 Torr to 1×10^{-3} Torr
Accuracy: 0.5%
Response: 10ms

Viscous-Drag

Range: 1×10^{-1} Torr to 1×10^{-6} Torr
Accuracy: 3%
Response: seconds

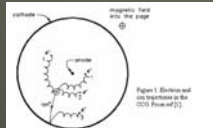
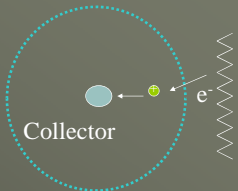


Measure time from 415-405Hz

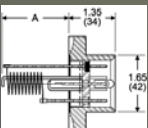
Ionization Gauge

2 types

- Hot Cathode (Ion Gauge)
- Cold Cathode (Penning Gauge)





Range: 1×10^{-3} to 1×10^{-10} Torr
Response: ms



Other Gauges

Mass Spectrometry (RGA)



Range: 1×10^{-5} to 1×10^{-14} Torr
Accuracy .01%
Response: ms

Pumps

3 Types

1. Mechanical
2. Diffusion
3. Entrainment

Mechanical Pumps

1. Rotary Vane Pumps
2. Roots Blower
3. Scroll Pump
4. Diaphragm Pumps
5. Molecular Drag Pump
6. Turbomolecular Pump

Rough Pumps
 Atm-100mTorr

1 - 1×10^{-6} Torr
 1×10^{-3} - 1×10^{-8} Torr

Rough Pumps

Rotary Type Blower

Turbo Pumps

Diffusion

Vapor Jet

Cooling

To Rough Pump

Oil, Heater

Vapor Jet

50-50000 L/s

Entrainment

1. Sorption Pumps
2. Getter Pumps
3. Cryopumps
4. Ion Pumps

Getters and Ion

GM + O₂ → GMO
 GM + N₂ → GMN
 GM + CO₂ → CO + GMO → GMC + GMO
 GM + CO → GMC + GMO
 GM + H₂O → H + GMO → GMO + H (bulk)
 GM + H₂ → GM + H (bulk)
 GM + Hydrocarbons, C_nH_m, etc. → GMC + H (bulk)
 GM + He, Ne, Ar, Kr, Xe (inert gases) → No Reaction

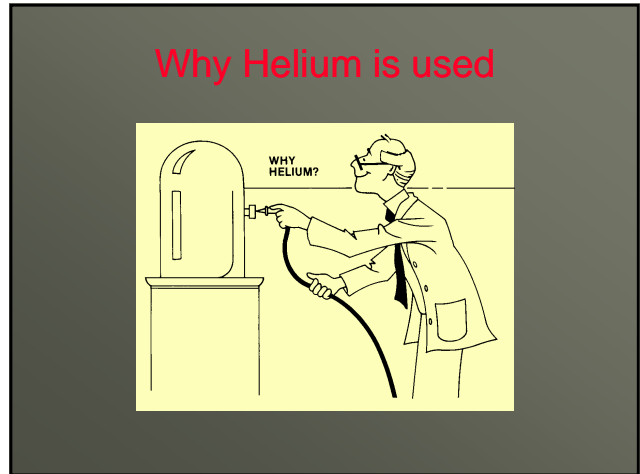
Getter pellet with clean surface, active gas molecule approaching

Getter pellet with active gas molecule adsorbed on surface

Getter pellet with active gas molecule diffused into bulk by heating

Cryo Pumps

Materials	
Quartz and Pyrex	UHV – He Leak
Ceramics – Alumina	Good internal parts
Brass	Contains Zinc – Outgasses at 10^{-6}
Copper and Oxygen Free	Oxygen free reduces outgassing for heating
Stainless Steel 300 series (304, 316)	Weldable
Aluminum 6000 series	Porous and Oxide surface – outgasses better than stainless
Plastic	Outgas at 10^{-7} Polyimide, Delron, Kapton – Good Be careful of wiring shield



- ## HELIUM
- ◆ Helium is very light and small
 - ◆ Low concentration in air (0.0005%)
 - ◆ Permits dynamic testing
 - ◆ Permits non-destructive testing
 - ◆ Helium is safe



